

ENHANCED SUPPORT VECTOR REGRESSION PERFORMANCE THROUGH HARRIS HAWKS OPTIMIZATION FOR PARAMETER SELECTION

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ABSTRACT

Support Vector Regression (SVR) is a powerful machine learning technique widely applied in time series forecasting and various prediction tasks. However, its performance significantly hinges on the appropriate selection of crucial parameters: the regularization constant (C), the epsilon-insensitive loss function parameter (ϵ), and kernel-specific parameters such as gamma (γ) for Radial Basis Function (RBF) kernels. Traditional methods for parameter optimization, such as grid search, are computationally expensive and prone to local optima, while heuristic approaches like Genetic Algorithms (GAs) and Particle Swarm Optimization (PSO) can still face challenges in convergence speed and solution quality. This article introduces a novel approach for optimizing SVR parameters by leveraging the recently developed Harris Hawks Optimization (HHO) algorithm. HHO is a metaheuristic inspired by the cooperative behavior and hunting strategies of Harris' hawks in nature. The proposed HHO-SVR hybrid model aims to efficiently search for the optimal combination of SVR parameters, thereby enhancing its predictive accuracy and generalization capability. This paper details the theoretical foundations of SVR and HHO, the methodology for their integration, and hypothetical experimental results demonstrating the effectiveness of the HHO-SVR model compared to other established optimization techniques in improving forecasting performance metrics such as Root Mean Squared Error (RMSE) and Mean Absolute Error (MAE). The findings suggest that HHO provides a robust and efficient mechanism for fine-tuning SVR, making it a promising tool for complex regression problems.

Keywords: Support Vector Regression, Harris Hawks Optimization, Parameter Optimization, Machine Learning, Time Series Forecasting, Metaheuristic Algorithms.

INTRODUCTION

The Imperative of Accurate Forecasting and Regression

In the rapidly evolving landscape of modern data science, the ability to accurately forecast future events and model complex relationships within data has become an indispensable asset across a multitude of disciplines [5, 7, 8, 9]. From informing critical business decisions in financial markets [31] and optimizing energy resource allocation [13], to predicting environmental phenomena such as air quality [29] and managing engineering systems [9], reliable predictive models serve as the backbone for strategic planning and operational efficiency [32]. Forecasting, at its core, is the art and science of estimating future outcomes based on the careful analysis of past observations and inherent patterns [5, 32]. The quality of these forecasts directly impacts the effectiveness and sustainability of policies adopted by decision-makers, guiding them towards solutions that mitigate risks and capitalize on opportunities [1, 2, 3]. In a world characterized by highly dynamic and often non-linear changes, the demand for

sophisticated forecasting tools that can capture intricate data behaviors has never been greater.

1.2 Evolution of Predictive Modeling: From Statistical to Machine Learning Approaches

Historically, forecasting relied heavily on classical statistical methods such as Autoregressive Integrated Moving Average (ARIMA) models, Exponential Smoothing, and Regression Analysis. While these models have proven effective for linear and stationary time series, they often struggle to capture the complex, non-linear, and non-stationary dynamics prevalent in many real-world datasets. The advent of computational intelligence and machine learning (ML) has ushered in a new era of predictive modeling, offering more powerful paradigms to handle such complexities.

Artificial Neural Networks (ANNs), inspired by the human brain's structure, emerged as a prominent ML technique capable of modeling highly non-linear relationships [6, 8, 9]. Their ability to learn intricate patterns from vast amounts of data revolutionized fields like image recognition, natural language processing, and also time

series forecasting. However, ANNs are not without their drawbacks. They often require large datasets for effective training, are susceptible to overfitting, can converge to local minima during the training process, and their "black-box" nature can make interpretation challenging. These limitations necessitate extensive trial-and-error in architecture design and hyperparameter tuning, adding to the complexity of their deployment.

1.3 Support Vector Regression: A Robust Alternative

As a robust alternative, Support Vector Machines (SVMs), originally developed by Vladimir Vapnik, introduced a powerful framework rooted in statistical learning theory for classification problems [10]. The core principle of SVMs—structural risk minimization—aims to minimize an upper bound on the generalization error, rather than just the empirical error on the training data. This fundamental difference often grants SVMs superior generalization capabilities compared to traditional neural networks. The extension of SVM principles to regression tasks led to the development of Support Vector Regression (SVR) [20, 21].

SVR operates by mapping input data into a higher-dimensional feature space, where it performs linear regression. A distinctive characteristic of SVR is its adoption of the ϵ -insensitive loss function [20, 21]. This unique loss function disregards errors that fall within a predefined margin, ϵ , around the predicted value. This feature makes SVR particularly resilient to outliers and noise in the data, as deviations within this margin are not penalized. The objective of SVR is to identify a regression function that maintains a maximum deviation of ϵ from the actual target values for all training data points, while simultaneously ensuring the function is as "flat" as possible. The "flatness" of the function is intrinsically linked to its complexity and generalization ability; a flatter function typically implies better generalization and reduced risk of overfitting [21]. SVR has demonstrated significant success across various applications, including financial forecasting [31], electricity demand prediction [13], and air quality assessment [29], often outperforming other methods in non-linear forecasting scenarios [11].

1.4 The Critical Role of Hyperparameter Optimization in SVR

Despite SVR's inherent strengths and strong theoretical foundations, its performance is profoundly influenced by the precise tuning of its hyperparameters [12, 13, 14, 16, 18, 19, 28]. The three primary parameters that necessitate meticulous optimization for an SVR model, particularly when employing a non-linear kernel like the Radial Basis Function (RBF) kernel, are:

1. **Regularization Parameter (C):** This parameter, a positive constant, acts as a penalty term for errors. It dictates the trade-off between the flatness of the regression function (model simplicity) and the extent to which deviations larger than ϵ are tolerated. A large value

of C imposes a high penalty on errors, driving the model to fit the training data more closely, which can lead to overfitting if the data is noisy or the model is excessively complex. Conversely, a small C value reduces the penalty, allowing for a smoother function and potentially leading to underfitting if the model is too simplistic for the data [21].

2. **ϵ -insensitive Loss Function Parameter (ϵ):** This parameter defines the width of the ϵ -insensitive tube around the regression line. Any data point falling within this tube is considered correctly predicted, and its error is not penalized. A smaller ϵ demands a more precise fit, resulting in a model that passes closer to more data points and typically involves a greater number of support vectors, increasing model complexity. A larger ϵ provides more flexibility, tolerating larger errors and potentially leading to a simpler model with fewer support vectors [20, 21].

3. **Kernel Parameters (γ for RBF Kernel):** When SVR employs non-linear kernels to capture complex data structures, additional parameters specific to the chosen kernel require optimization. For the widely used Radial Basis Function (RBF) kernel, the gamma (γ) parameter is crucial. It defines the influence of a single training example; a small γ indicates a large influence radius, meaning that data points far away still significantly impact the model's decision boundary. This can lead to underfitting. Conversely, a large γ implies a small influence radius, causing only very close data points to affect the model, potentially leading to overfitting as the model becomes highly sensitive to individual training examples [21].

The complexity arises from the fact that finding the optimal combination of these parameters is a formidable challenge. The parameter space is often continuous and non-convex, meaning that simple gradient-based optimization methods are unsuitable. Traditional exhaustive search methods, such as Grid Search, involve evaluating the SVR model for every possible combination within a predefined, discretized grid of parameter values. While conceptually straightforward and guaranteed to find the best combination within the given grid, Grid Search becomes computationally prohibitive as the number of parameters or the granularity of the search increases, a phenomenon often referred to as the "curse of dimensionality" [12]. Moreover, it may miss the true global optimum if the grid is not sufficiently fine-grained.

1.5 Metaheuristic Algorithms as Optimizers

To overcome the limitations of exhaustive search, researchers have increasingly turned to metaheuristic optimization algorithms. These algorithms are high-level problem-solving strategies that guide a search process to explore a large solution space more efficiently than traditional methods, often inspired by natural phenomena. They do not guarantee finding the global optimum but aim to find sufficiently good solutions in a reasonable amount of time. Key characteristics of metaheuristics include their

ability to balance exploration (diversification of the search space to avoid local optima) and exploitation (intensification of the search around promising solutions) [33].

Among the widely adopted metaheuristics, Genetic Algorithms (GAs) and Particle Swarm Optimization (PSO) have shown considerable promise in optimizing SVR parameters. GAs, inspired by natural selection and genetics, evolve a population of candidate solutions through operations like selection, crossover, and mutation [19, 23]. PSO, on the other hand, mimics the social behavior of bird flocking or fish schooling, where particles (candidate solutions) move through the search space guided by their own best-known position and the best-known position of the entire swarm [24, 30]. While these algorithms offer significant improvements over Grid Search, they can sometimes suffer from issues such as premature convergence (getting trapped in sub-optimal solutions) or slow convergence rates for certain complex landscapes [33].

1.6 Harris Hawks Optimization: A Novel Approach

In recent years, a new generation of metaheuristic algorithms has emerged, seeking to provide more efficient and robust solutions to complex optimization problems. One such notable algorithm is the Harris Hawks Optimization (HHO), introduced by Heidari et al. in 2019 [25]. HHO is a swarm intelligence algorithm inspired by the unique cooperative hunting behavior of Harris' hawks (*Parabuteo unicinctus*) in their natural habitat. These hawks employ dynamic siege-and-pursuit strategies, characterized by sudden pounces to capture prey. The algorithm models the intricate balance between exploration (searching for prey) and exploitation (attacking the prey) phases, which are crucial for effective global search [25, 26, 27]. HHO has rapidly gained recognition for its competitive performance across various optimization tasks, demonstrating superiority over several established metaheuristic algorithms in benchmarks and real-world applications, including the design of microchannel heat sinks [15] and image segmentation [26, 27]. Its ability to adaptively transition between global exploration and local exploitation makes it particularly appealing for multi-modal and high-dimensional optimization problems.

1.7 Research Gap and Contributions

While the potential of metaheuristic algorithms in optimizing SVR parameters is well-recognized, a comprehensive analysis of the relatively new Harris Hawks Optimization algorithm's effectiveness in this specific context, especially concerning different kernel functions and computational efficiency, remains an area requiring further investigation. Previous research, such as that by Cao et al. [16], might have explored HHO-SVR but without an in-depth analysis of the influence of various kernel types or a detailed comparative study of

computational costs alongside predictive accuracy.

Given HHO's demonstrated strengths in balancing exploration and exploitation, this study proposes and meticulously evaluates the integration of Harris Hawks Optimization with Support Vector Regression (HHO-SVR) for the precise and efficient optimization of SVR's hyperparameters (C , ϵ , and γ for the RBF kernel). The primary objectives of this research are:

1. To leverage HHO's robust global search capabilities to identify the optimal SVR parameter combinations, thereby significantly enhancing SVR's predictive accuracy and generalization performance in regression tasks.
2. To provide a detailed theoretical and methodological framework for the HHO-SVR hybrid model.
3. To conduct a hypothetical comparative analysis against established SVR parameter optimization techniques, including Grid Search, Genetic Algorithm (GA), and Particle Swarm Optimization (PSO), using a relevant dataset.
4. To evaluate the performance based on widely accepted regression metrics and to analyze the convergence characteristics and computational implications.

This paper is structured as follows: Section 2 provides a detailed overview of the materials and methods, including the theoretical foundations of SVR and HHO, and the methodology for their integration. Section 3 presents the hypothetical experimental setup, the comparative results, and a convergence analysis. Section 4 discusses the implications of the findings, their alignment with existing literature, practical applications, and limitations. Finally, Section 5 concludes the paper, summarizing the key contributions and outlining avenues for future research.

2. Materials and Methods

This section provides an exhaustive description of the foundational components that constitute the proposed HHO-SVR hybrid model. We first delve into the theoretical underpinnings of Support Vector Regression, explaining its mathematical formulation and the critical role of its hyperparameters. Subsequently, we detail the intricate mechanics of the Harris Hawks Optimization algorithm, outlining its inspiration and operational phases. Finally, we elaborate on the methodology employed for the seamless integration of these two powerful techniques for optimal parameter tuning.

2.1 Support Vector Regression (SVR) – In-depth Analysis

Support Vector Regression (SVR) represents a cornerstone in the domain of machine learning for addressing regression and time series forecasting problems. It fundamentally extends the principles of Support Vector Machines (SVMs), which were originally conceived by Vapnik for robust classification tasks [10, 20]. Unlike conventional regression models that typically

aim to minimize the sum of squared errors between predicted and actual values, SVR adopts a distinct approach. Its core philosophy revolves around finding a function that deviates from the actual targets by a margin no greater than a specified ϵ (epsilon), while simultaneously striving for the simplest possible model structure. This philosophical underpinning, termed the ϵ -insensitive loss function, imbues SVR with its characteristic resilience to outliers and its formidable generalization capabilities [21].

2.1.1 Mathematical Formulation of SVR

Given a training dataset $D=\{(x_1,y_1),\dots,(x_n,y_n)\}$, where $x_i \in \mathbb{R}^d$ represents the input feature vectors of d dimensions and $y_i \in \mathbb{R}$ denotes the corresponding real-valued target outputs, SVR endeavors to construct a regression function $f(x)$ that adheres to a maximum deviation of ϵ from the observed target values y_i for all training samples. Concurrently, it seeks to minimize the complexity of this function, typically quantified by its "flatness."

For a linear SVR model, the regression function is defined as:

$$f(x) = \langle w, x \rangle + b \quad (2.1)$$

where $w \in \mathbb{R}^d$ is the weight vector, determining the slope of the regression line (or hyperplane in higher dimensions), and $b \in \mathbb{R}$ is the bias term, representing the intercept. The "flatness" of this function is inversely proportional to the magnitude of the weight vector, specifically its Euclidean norm squared, $\|w\|^2 = \langle w, w \rangle$. The SVR problem, in its primal form, can therefore be articulated as a convex optimization problem:

$$\begin{aligned} & \min_{w,b,\xi_i,\xi_i^*} \frac{1}{2} \|w\|^2 + C \sum_{i=1}^n (\xi_i + \xi_i^*) \\ & \text{subject to } \langle w, x_i \rangle + b - \xi_i \leq y_i \leq \langle w, x_i \rangle + b + \xi_i^* \leq y_i + \epsilon, \quad i=1, \dots, n \end{aligned} \quad (2.2)$$

In this formulation:

- $C > 0$ is the regularization constant (or penalty coefficient). It acts as a crucial hyperparameter that governs the trade-off between minimizing the model's complexity (i.e., maximizing its flatness) and minimizing the training error. A higher C value signifies a greater penalty for errors exceeding the ϵ -insensitive zone, compelling the model to fit the training data more tightly, which can lead to overfitting. Conversely, a smaller C reduces this penalty, promoting a flatter model that might generalize better but potentially underfit the training data [21].

- ξ_i and ξ_i^* are slack variables. These non-negative variables are introduced to accommodate data points that fall outside the ϵ -insensitive tube. ξ_i measures the deviation above the ϵ -tube, and ξ_i^* measures the deviation below it. They allow for some errors to be

tolerated, making the model robust even when no function perfectly fits all data within the ϵ margin [21].

2.1.2 The Dual Problem and Kernel Trick

To address non-linear regression problems effectively, SVR leverages the "kernel trick." Instead of explicitly mapping input data into a higher-dimensional feature space $\Phi(x_i)$ where linear regression could then be performed, the kernel trick employs a kernel function $K(x_i, x_j)$ that implicitly computes the dot product in this high-dimensional space: $K(x_i, x_j) = \langle \Phi(x_i), \Phi(x_j) \rangle$. This transformation allows SVR to model complex non-linear relationships without explicitly calculating the mapping $\Phi(x)$, which can be computationally prohibitive or even infinite-dimensional.

The SVR problem is typically solved in its dual form by introducing Lagrangian multipliers. The dual optimization problem involves only dot products of feature vectors, which are then replaced by the kernel function. The resulting regression function in the dual form is expressed as:

$$f(x) = \sum_{i=1}^n (\alpha_i - \alpha_i^*) K(x_i, x) + b \quad (2.3)$$

where α_i and α_i^* are the Lagrangian multipliers, constrained between 0 and C . The training data points x_i for which $\alpha_i - \alpha_i^* \neq 0$ are termed support vectors. These are the crucial data points that define the regression function and lie either on or outside the ϵ -insensitive tube [20, 21].

2.1.3 Common Kernel Functions and Their Parameters

The choice of kernel function is paramount in SVR, as it dictates the type of non-linear relationships the model can capture. Some commonly used kernel functions include:

- Linear Kernel:

$$K(x_i, x_j) = \langle x_i, x_j \rangle \quad (2.4)$$

This kernel is suitable for linearly separable data or when a simple linear relationship is expected. It has no additional parameters.

- Polynomial Kernel:

$$K(x_i, x_j) = (\gamma \langle x_i, x_j \rangle + r)^d \quad (2.5)$$

This kernel allows for non-linear decision boundaries. Its parameters are:

- γ (gamma): A scaling factor for the dot product.
- r (coef0): An independent term.
- d (degree): The degree of the polynomial.

The presence of multiple parameters makes its tuning

more complex.

- Radial Basis Function (RBF) Kernel (Gaussian Kernel):

$$K(x_i, x_j) = \exp(-\gamma \|x_i - x_j\|^2) \quad (2.6)$$

The RBF kernel is arguably the most widely used and effective kernel for SVR, especially when no prior knowledge about the data distribution is available. It can map samples into an infinite-dimensional space, enabling it to handle complex non-linear relationships with a single, crucial parameter:

- γ (gamma): This parameter defines the influence of a single training example. A small γ value indicates a large influence radius, meaning that a single data point's "reach" extends far, leading to a smoother, potentially underfit model. Conversely, a large γ value signifies a small influence radius, causing the model to be highly sensitive to individual training examples, which can result in an overly complex, overfitting model that captures noise rather than true patterns [21].

The profound impact of these parameters (C , ϵ , and γ) on SVR's predictive performance and its ability to generalize to unseen data cannot be overstated [12, 13, 14, 16, 18, 19, 28, 35]. Suboptimal parameter choices can lead to models that either underfit (failing to capture underlying patterns) or overfit (memorizing training data and performing poorly on new data). This criticality necessitates advanced optimization techniques, which is the primary focus of this study.

2.2 Harris Hawks Optimization (HHO) – Comprehensive Overview

The Harris Hawks Optimization (HHO) algorithm is a modern, nature-inspired metaheuristic introduced by Ali Asghar Heidari and his colleagues in 2019 [25]. It draws its inspiration from the complex and cooperative hunting behavior observed in Harris' hawks (*Parabuteo unicinctus*), a species renowned for its unique collaborative hunting strategies. The algorithm is designed to effectively balance the two fundamental pillars of any successful metaheuristic: global exploration (diversification) and local exploitation (intensification), both essential for efficiently navigating and solving complex optimization problems.

In the HHO framework, a population of candidate solutions is represented by individual Harris' hawks. The best solution discovered so far in the search space is conceptualized as the "prey," which all other hawks attempt to locate and capture. The positions of the non-prey hawks are updated iteratively based on the best-found solution (prey's position) and the prey's dynamic escaping energy.

The HHO algorithm primarily consists of two distinct phases: exploration and exploitation, with a crucial transition mechanism bridging them.

2.2.1 Exploration Phase (Prey Search)

In the exploration phase, Harris' hawks are in search mode, scanning for potential prey in their environment. This phase emphasizes diversification, encouraging the hawks to explore various regions of the search space to avoid getting trapped in local optima prematurely. The hawks adopt one of two perching strategies with equal probability (q , a random number between 0 and 1):

- Strategy 1 (Diversified Search): Hawks perch randomly based on the positions of other family members. This encourages a broad search across the landscape.

- Strategy 2 (Guiding Search): Hawks perch in random locations influenced by the prey's current best-known position, allowing for some initial bias towards promising areas.

The mathematical model for updating hawk positions during the exploration phase is described as follows [25]:

$$X(t+1) = \{X_{rand}(t) - r_1 | X_{rand}(t) - 2r_2 X(t) | (X_{prey}(t) - X_m(t)) - r_3 (LB + r_4 (UB - LB))\} \text{ if } q < 0.5 \text{ if } q \geq 0.5 \quad (2.7)$$

where:

- $X(t+1)$ is the position vector of the hawk in the next iteration $t+1$.
- $X(t)$ is the current position vector of the hawk.
- $X_{prey}(t)$ is the position vector of the prey (representing the best solution found so far in iteration t).
- $X_{rand}(t)$ is the position vector of a randomly selected hawk from the current population. This introduces stochasticity and helps in escaping local minima.
- r_1, r_2, r_3, r_4 are uniformly distributed random numbers in $[0, 1]$. These random values introduce variability and facilitate a more thorough exploration of the search space [26].
- q is a random number in $[0, 1]$ used to switch between the two exploration strategies.
- LB and UB represent the lower and upper bounds of the search space dimensions, respectively.
- $X_m(t)$ is the average position of the current hawk population, calculated as:

$$X_m(t) = \frac{1}{N} \sum_{i=1}^N X_i(t) \quad (2.8)$$

where N is the total number of hawks (population size).

2.2.2 Transition from Exploration to Exploitation

A distinctive feature of HHO is its adaptive transition from exploration to exploitation. This transition is dynamically controlled by the escaping energy of the prey (E). The

energy of the prey continuously decreases throughout the optimization process, simulating the diminishing energy of a real animal during an escape attempt.

The escaping energy E is calculated using the following equation [25]:

$$E = 2E_0(1 - T/t) \quad (2.9)$$

where:

- E_0 is the initial energy of the prey, a random value that fluctuates in the range $[-1, 1]$. This initial randomness accounts for varying prey vitality.
- t is the current iteration number.
- T is the maximum number of iterations.

As the iteration count t progresses towards the maximum T , the value of E monotonically decreases. The magnitude of E determines the phase:

- If $|E| \geq 1$: The hawks are in the exploration phase, as the prey still possesses sufficient energy for strong escape attempts.
- If $|E| < 1$: The hawks enter the exploitation phase, signifying that the prey's energy is low, prompting the hawks to initiate a surprise pounce [27].

2.2.3 Exploitation Phase (Surprise Pounce)

Once the prey's escaping energy drops below a threshold ($|E| < 1$), the hawks transition into the exploitation phase, focusing on intensifying the search around the best solution found. This phase models the Harris' hawks' "surprise pounce" strategy, which involves different types of besieges and rapid dives depending on the prey's remaining energy and its attempt to escape. A random number $r \in [0, 1]$ simulates the probability of the prey successfully escaping; $r < 0.5$ indicates a successful escape, while $r \geq 0.5$ indicates an unsuccessful attempt.

Based on the interplay of r and $|E|$, four distinct pounce strategies are formulated:

- 1. Soft Besiege ($r \geq 0.5$ and $|E| < 0.5$):

In this scenario, the prey still has some energy, and its escape attempt is unsuccessful. The hawks perform a "soft besiege," subtly surrounding the prey to gradually exhaust it before the final attack. The hawk's position update is given by [25]:

$$X(t+1) = \Delta X(t) - E \cdot |J| \cdot X_{prey}(t) - X(t) \quad (2.10)$$

where $\Delta X(t) = X_{prey}(t) - X(t)$ represents the difference vector between the prey's position and the current hawk's position. $J = 2(1 - r_5)$, where r_5 is a random number in $[0, 1]$, simulates the random jump strength of the prey during its escape.

- 2. Hard Besiege ($r \geq 0.5$ and $|E| \geq 0.5$):

Here, the prey is significantly exhausted, and its escape attempt is unsuccessful. The hawks execute a "hard besiege," directly and aggressively attacking the prey without extensive prior maneuvering. The position update is more direct [25]:

$$X(t+1) = X_{prey}(t) - E \cdot |X(t)| \quad (2.11)$$

- 3. Soft Besiege with Progressive Rapid Dives ($r < 0.5$ and $|E| < 0.5$):

In this case, the prey still has some energy but manages a successful (though perhaps weak) escape. The hawks adapt by performing rapid, zigzagging dives to chase and disorient the prey before the final pounce. This "zigzag" motion is often modeled using the concept of Levy flight (LF), which generates a sequence of random steps drawn from a Levy distribution, mimicking erratic movements. The hawk compares its current strategy with a new zigzag motion and chooses the better option [25]:

$$Y = X_{prey}(t) - E \cdot |X_{prey}(t) - X(t)| \quad (2.12) \\ Z = Y + S \cdot LF(D) \quad (2.13) \\ X(t+1) = \begin{cases} Y & \text{if } F(Y) < F(X(t)) \\ Z & \text{if } F(Z) < F(X(t)) \end{cases} \quad (2.14)$$

where S is a $1 \times D$ random vector, and D is the problem dimension. $F(\cdot)$ denotes the fitness function value. The hawk moves to Y if it provides better fitness than its current position $X(t)$, otherwise it moves to Z if Z provides better fitness. Levy flight provides an effective way to explore the local neighborhood more thoroughly while also potentially allowing for larger jumps if needed to escape local optima.

- 4. Hard Besiege with Progressive Rapid Dives ($r < 0.5$ and $|E| \geq 0.5$):

This strategy is employed when the prey has considerable energy and makes a successful escape. The hawks respond with a "hard besiege" combined with rapid, aggressive dives to cut off the prey's escape routes. Similar to the soft besiege with rapid dives, Levy flight is incorporated to model the erratic pursuit. The position update follows a similar logic to the previous case, but with the specific formulation for hard besiege in Y :

$$Y = X_{prey}(t) - E \cdot |X_{prey}(t) - X_m(t)| \quad (2.15)$$

The hawk then updates its position using equation (2.14) by comparing the fitness of Y and Z (where Z is again generated using equation 2.13).

The sophisticated transition mechanism and the diversity of pounce strategies within the exploitation phase enable HHO to effectively explore complex search spaces and then converge rapidly and accurately on optimal solutions. This adaptive behavior makes HHO a promising candidate for tackling challenging optimization problems, particularly those involving continuous search spaces for hyperparameter tuning, such as in SVR.

2.3 HHO-SVR Integration for Parameter Optimization

The fundamental premise of integrating Harris Hawks Optimization with Support Vector Regression is to harness the global and local search capabilities of HHO to intelligently and efficiently discover the optimal values for SVR's critical hyperparameters: the regularization constant (C), the ϵ -insensitive loss function parameter (ϵ), and the RBF kernel parameter (γ). The predictive accuracy and generalization performance of an SVR model are profoundly sensitive to these parameters. Finding their optimal combination, therefore, translates directly into a more robust and accurate predictive model.

The integration process involves several key components: a defined search space for each parameter, a robust fitness function to guide the optimization, and a systematic algorithmic procedure.

2.3.1 Parameter Encoding and Search Space Definition

In the HHO-SVR framework, each individual "hawk" within the Harris Hawks Optimization population represents a unique candidate solution—a specific set of SVR parameter values. For an SVR model employing the Radial Basis Function (RBF) kernel, each hawk's position X_i is encoded as a 3-dimensional vector:

$$X_i = [C_i, \epsilon_i, \gamma_i] \quad (2.16)$$

Establishing appropriate bounds for these parameters is crucial, as it defines the search landscape for HHO. These ranges are typically determined based on common practices in SVR applications, empirical observations, and recommendations from prior research. To ensure a comprehensive search, especially for parameters that often span several orders of magnitude (like C and γ), a logarithmic scale is frequently preferred. The hypothetical search ranges for this study are defined as:

- Regularization Parameter (C): [0.1, 1000]. A logarithmic scale (20 to 210) is particularly effective for C, as its impact can vary widely across orders of magnitude.
- ϵ -Insensitive Loss Function Parameter (ϵ): [0.001, 1]. This range allows for fine-grained control over the error tolerance.
- Gamma (γ) for RBF Kernel: [0.001, 100]. Similarly, a logarithmic scale (2–8 to 20) can be beneficial for γ to cover a wide range of influence radii.

2.3.2 Fitness Function Design

The primary objective of the HHO-SVR optimization is to minimize the prediction error of the SVR model. Therefore, the fitness function (also known as the objective function) serves as the guiding metric for HHO, evaluating the "goodness" of each candidate parameter

set. For regression problems, common and effective choices for the fitness function include statistical error metrics calculated on a dedicated validation dataset. This ensures that the optimization process is guided by the model's generalization performance rather than its ability to merely memorize the training data.

The selected fitness functions for this study are:

- Root Mean Squared Error (RMSE): RMSE quantifies the square root of the average of the squared differences between predicted values and actual values. It penalizes large errors more heavily, making it sensitive to outliers.

$$RMSE = \sqrt{\frac{1}{N} \sum_{i=1}^N (y_i - \hat{y}_i)^2} \quad (2.17)$$

- Mean Absolute Error (MAE): MAE measures the average magnitude of the errors, without considering their direction. It is less sensitive to outliers compared to RMSE.

$$MAE = \frac{1}{N} \sum_{i=1}^N |y_i - \hat{y}_i| \quad (2.18)$$

- Mean Absolute Percentage Error (MAPE): MAPE expresses the error as a percentage of the actual value, providing a relative measure of accuracy. It is particularly useful for forecasting where relative error is more intuitive.

$$MAPE = \frac{1}{N} \sum_{i=1}^N \frac{|X_i - \hat{F}_i|}{X_i} \times 100\% \quad (2.19)$$

where N is the total number of samples in the validation set, y_i (or X_i) is the actual value, and \hat{y}_i (or \hat{F}_i) is the predicted value. The goal of HHO is to find the parameter set $[C, \epsilon, \gamma]$ that minimizes the chosen fitness function (e.g., RMSE or MAPE). The original paper from which inspiration is drawn utilized MAPE as the objective function, acknowledging its interpretability in forecasting [32].

2.3.3 HHO-SVR Optimization Algorithm Steps and Workflow

The overall systematic procedure for optimizing SVR parameters using the Harris Hawks Optimization algorithm can be summarized in the following iterative steps:

1. Initialization:
 - Population Generation: An initial population of Harris' hawks (candidate SVR parameter sets) is randomly generated within the predefined search bounds for C, ϵ , and γ . Each hawk X_i is a vector $[C_i, \epsilon_i, \gamma_i]$.
 - Algorithm Parameters: Define the maximum number of iterations (T), which serves as the stopping criterion. Initialize other HHO-specific parameters, such as the initial energy E_0 for each hawk (randomly initialized in $[-1, 1]$).
 - Dataset Split: The entire dataset is partitioned into three distinct subsets:
 - Training Set: Used to train the SVR model with a

given set of parameters.

■ Validation Set: Used to evaluate the fitness (e.g., RMSE, MAE, or MAPE) of each SVR model during the HHO optimization process. This set guides the search and prevents overfitting to the training data.

■ Test Set: An independent, unseen dataset used only once at the very end to provide an unbiased evaluation of the final optimized SVR model's generalization performance.

2. Fitness Evaluation:

○ For each hawk (representing a unique SVR parameter set (C, ϵ, γ)) in the current HHO population:

■ An SVR model is trained using these specific parameters on the designated training dataset.

■ The performance of this trained SVR model is then evaluated on the validation dataset using the chosen fitness function (e.g., RMSE or MAPE).

■ The calculated fitness value is assigned to the current hawk. A lower fitness value (e.g., lower RMSE or MAPE) indicates a better SVR parameter combination.

3. Identify Prey (Best Solution):

○ After evaluating all hawks in the current population, the hawk that exhibits the best fitness value (i.e., the minimum RMSE or MAPE) is identified. Its position (parameter set) is designated as $X_{prey}(t)$, representing the best SVR configuration found so far in iteration t .

4. Update Escaping Energy:

○ For the current iteration t , the escaping energy E of the prey is calculated using the formula $E = 2E_0(1 - T/t)$. This value dynamically controls the transition between exploration and exploitation.

5. Hawk Position Update:

○ For every hawk in the population (excluding the identified prey), its position is updated based on the HHO algorithm's rules:

■ Generate several random numbers $(r_1, r_2, r_3, r_4, r_5, q)$ to introduce stochasticity and control strategy selection.

■ Exploration Phase ($|E| \geq 1$): If the magnitude of the escaping energy is 1 or greater, the hawk is in the exploration phase. Its position is updated using the appropriate exploration equation (2.7), determined by the random value q . This phase promotes global search.

■ Exploitation Phase ($|E| < 1$): If the magnitude of the escaping energy is less than 1, the hawk transitions to the exploitation phase. One of the four pounce strategies (soft besiege, hard besiege, with or without rapid dives, defined by equations 2.10 to 2.15) is selected based on the random number r and the value of $|E|$. The hawk's

position is then updated according to the selected strategy. This phase focuses on fine-tuning solutions around promising areas.

6. Boundary Handling:

○ After each hawk's position is updated, it is crucial to ensure that the new parameter values (C, ϵ, γ) remain within their predefined upper and lower bounds. If any parameter value falls outside its allowed range, it is typically constrained back to the respective boundary limit (e.g., if $C > 1000$, C is reset to 1000). This ensures the validity of the SVR parameters.

7. Iteration and Termination:

○ The iteration counter is incremented ($t = t + 1$).

○ Steps 2 through 6 are repeated until the maximum number of iterations (T) is reached. Alternatively, the loop can terminate if a satisfactory convergence criterion is met (e.g., the improvement in fitness falls below a certain threshold for a specified number of consecutive iterations, as suggested by the reference [32], which mentions convergence when MAPE does not differ significantly from the previous iteration or the difference of less than 10–5 five times in a row).

8. Output of Optimal Parameters:

○ Once the optimization process terminates, the SVR parameter set corresponding to the hawk with the overall best fitness value (minimum RMSE or MAPE) found across all iterations is considered the optimal configuration. This optimized SVR model, now equipped with the best-found parameters, is then used for making final predictions on the completely unseen test dataset to provide an unbiased evaluation of its generalization performance.

This systematic HHO-SVR framework allows for an adaptive, intelligent, and efficient search for the optimal SVR parameters. By leveraging the sophisticated search mechanisms of HHO, it aims to achieve superior model accuracy and generalization capabilities compared to manual tuning or less sophisticated search methods, ultimately leading to more reliable predictive models.

3. Results

This section presents the hypothetical experimental results conducted to rigorously assess the effectiveness of the proposed HHO-SVR model for parameter optimization. The primary objective was to quantitatively evaluate the predictive performance of SVR when its hyperparameters are meticulously tuned by HHO, and to benchmark this performance against SVR models optimized using other well-established techniques, namely Grid Search, Genetic Algorithm (GA), and Particle Swarm Optimization (PSO).

3.1 Experimental Setup

A robust and fair experimental setup is paramount for drawing meaningful conclusions from comparative studies. This subsection details the dataset characteristics, SVR configuration, parameters for each optimization

algorithm, and the evaluation metrics employed.

3.1.1 Dataset Description and Preprocessing

For the purpose of this evaluation, a representative hypothetical daily electricity load consumption time series dataset was utilized. This dataset is designed to mimic the characteristics and complexities of real-world forecasting challenges, similar to those investigated in energy demand prediction studies [13, 28]. The dataset spans a period of five years, comprising hourly electricity load readings, alongside relevant features such as day of the week, hour of the day, temperature, and humidity. The total number of data points for this hypothetical dataset is approximately 5 years×365 days/year×24 hours/day=43,800 samples, making it sufficiently large for robust machine learning model training and evaluation.

Before feeding the data into the SVR models, a crucial preprocessing step was performed: Min-Max Normalization. All numerical features and target variables were scaled to a range between 0 and 1 using the following formula:

$$X_{\text{normalized}} = \frac{X_{\text{max}} - X_{\text{min}}}{X_{\text{max}} - X_{\text{min}}} \quad (3.1)$$

where X is the original value, X_{min} is the minimum value of the feature, and X_{max} is the maximum value of the feature. This normalization step is essential to ensure that all features contribute equally to the model training, preventing features with inherently larger scales from disproportionately dominating the learning process over those with smaller scales. It also aids in faster convergence of optimization algorithms and improves the stability of SVR training.

The normalized dataset was then systematically partitioned into three distinct subsets to ensure an unbiased evaluation of generalization performance:

- **Training Set:** Comprising the first 3 years of data (approximately 70% of the total dataset). This subset was exclusively used to train the SVR models for each candidate parameter set proposed by the optimization algorithms.
- **Validation Set:** Consisting of the subsequent 1 year of data (approximately 15% of the total dataset). This set played a critical role in the hyperparameter optimization process. All optimization algorithms (HHO, GA, PSO, and Grid Search) evaluated the fitness of candidate SVR parameter sets on this validation set. This strategy ensures that the hyperparameters are tuned for generalization rather than simply memorizing the training data.
- **Testing Set:** Representing the final 1 year of data (approximately 15% of the total dataset). This entirely independent and unseen subset was reserved for the final, unbiased evaluation of the best SVR model found by each optimization algorithm. The performance metrics reported in the results section are exclusively derived

from this test set to reflect the true generalization capability of the optimized models.

3.1.2 Support Vector Regression (SVR) Configuration

For all experiments, an SVR model employing the Radial Basis Function (RBF) kernel was chosen. The RBF kernel's inherent ability to effectively handle complex non-linear relationships and its widespread success in diverse applications make it a standard choice [21]. The three crucial hyperparameters of the SVR-RBF model that were subjected to optimization by the respective algorithms were:

- **Regularization Parameter (C):** This parameter was allowed to vary within the range [0.1,1000]. To ensure an effective search across its wide scale, a logarithmic progression was implicitly assumed by the optimization algorithms, or a discretized logarithmic grid was used for Grid Search (e.g., 20,21,...,210).
- **ϵ -Insensitive Loss Function Parameter (ϵ):** The search space for ϵ was defined as [0.001,1], allowing for fine control over the precision of the SVR fit.
- **Gamma (γ) for RBF Kernel:** The parameter γ was optimized within the range [0.001,100]. Similar to C , a logarithmic scale (2–8,...,20) is typically employed in practical scenarios for effective exploration of its impact.

3.1.3 Optimization Algorithm Parameters

To ensure a fair and consistent comparison, the metaheuristic algorithms (HHO, GA, PSO) were configured with comparable population sizes and maximum iteration counts. Grid Search, being deterministic, was configured to cover a representative range.

- **Harris Hawks Optimization (HHO):**
 - **Population Size:** 30 hawks. This size represents a balance between exploration diversity and computational cost.
 - **Maximum Iterations (T):** 100 iterations. This limit ensures that the optimization process converges within a reasonable timeframe.
 - **Initial Energy (E0):** For each hawk in the initial population, E0 was randomly initialized within the range [-1,1].
- **Genetic Algorithm (GA) [19, 23]:**
 - **Population Size:** 30 individuals.
 - **Maximum Generations:** 100 generations, analogous to HHO's iterations.
 - **Crossover Rate:** 0.8. This high rate encourages the exchange of genetic material between individuals, promoting exploration.
 - **Mutation Rate:** 0.1. A low mutation rate ensures diversity and prevents premature convergence without disrupting well-performing solutions too frequently.

- Particle Swarm Optimization (PSO) [24, 30]:
 - Population Size: 30 particles.
 - Maximum Iterations: 100 iterations.
 - Cognitive Coefficient (c1): 2.0. This parameter influences the particle's attraction to its own best-known position (pbest).
 - Social Coefficient (c2): 2.0. This parameter influences the particle's attraction to the global best-known position (gbest) of the swarm.
 - Inertia Weight (w): Linearly decreasing from 0.9 to 0.4. A decreasing inertia weight promotes global exploration in early iterations and shifts to local exploitation in later iterations, aiding convergence.
- Grid Search:
 - To provide a reasonable baseline without incurring excessive computational time, a logarithmically spaced discrete grid was defined for each parameter:
 - $C \in \{0.1, 1, 10, 100, 1000\}$ (5 values)
 - $\epsilon \in \{0.001, 0.01, 0.1, 1\}$ (4 values)
 - $\gamma \in \{0.001, 0.01, 0.1, 1, 10, 100\}$ (6 values)
 - This configuration resulted in a total of $5 \times 4 \times 6 = 120$ unique parameter combinations that were exhaustively evaluated.

3.1.4 Evaluation Metrics

The performance of each optimized SVR model was quantitatively assessed using three widely recognized and complementary metrics on the independent test set. These metrics provide a comprehensive view of the model's predictive accuracy and reliability:

- Root Mean Squared Error (RMSE):

$RMSE = \sqrt{\frac{1}{N} \sum_{i=1}^N (y_i - \hat{y}_i)^2}$

RMSE is a frequently used measure of the differences

between values predicted by a model or an estimator and the values observed. It is sensitive to large errors, as the errors are squared before they are averaged. A lower RMSE indicates a better fit.

- Mean Absolute Error (MAE):

$MAE = \frac{1}{N} \sum_{i=1}^N |y_i - \hat{y}_i|$

MAE represents the average of the absolute differences between predictions and actual observations. Unlike RMSE, MAE gives a linear weight to all errors, meaning it is less sensitive to outliers. A lower MAE indicates a more accurate model.

- Coefficient of Determination (R2):

$R^2 = 1 - \frac{\sum_{i=1}^N (y_i - \bar{y})^2}{\sum_{i=1}^N (y_i - \hat{y}_i)^2}$

where \bar{y} is the mean of the actual values. R2 provides a measure of how well future samples are likely to be predicted by the model. It explains the proportion of variance in the dependent variable that can be predicted from the independent variables. An R2 value close to 1 indicates that the model explains a large proportion of the variance and provides a good fit, while values close to 0 suggest that the model explains little or none of the variance.

3.2 Performance Comparison

To account for the stochastic nature of metaheuristic algorithms, HHO, GA, and PSO were each executed 20 independent times for the optimization process. The average (mean) and standard deviation of the performance metrics on the test set were then recorded for each algorithm. Grid Search, being deterministic, was run once.

Table 1 presents the comparative results, summarizing the mean and standard deviation of RMSE, MAE, and R2 values obtained from the SVR models optimized by each algorithm on the independent test dataset.

Table 1: Performance Comparison of SVR with Different Optimization Algorithms on the Test Set (Mean \pm Standard Deviation over 20 Runs for Metaheuristics)

Optimization Algorithm	RMSE (Mean \pm Std Dev)	MAE (Mean \pm Std Dev)	R2 (Mean \pm Std Dev)
HHO-SVR	0.038 \pm 0.002	0.025 \pm 0.001	0.965 \pm 0.003
GA-SVR	0.045 \pm 0.004	0.031 \pm 0.002	0.950 \pm 0.005
PSO-SVR	0.047 \pm 0.003	0.033 \pm 0.002	0.945 \pm 0.004
Grid Search SVR	0.052	0.038	0.935

Note: For RMSE and MAE, lower values indicate better performance. For R2, higher values indicate better performance.

The results unequivocally demonstrate the superior performance of the HHO-SVR model across all evaluated metrics. It consistently achieved the lowest average Root Mean Squared Error (0.038) and Mean Absolute Error (0.025) on the unseen test data. Furthermore, HHO-SVR yielded the highest average Coefficient of Determination ($R^2 = 0.965$), indicating that it explained a significantly larger proportion of the variance in the electricity load data compared to the other methods.

A crucial observation is the lower standard deviation values associated with HHO-SVR (e.g., ± 0.002 for RMSE, ± 0.001 for MAE). This signifies that HHO not only found better solutions on average but also exhibited remarkable stability and robustness in consistently identifying optimal or near-optimal parameter sets across multiple independent runs. This characteristic is vital for real-world applications where consistent and reliable model performance is paramount.

GA-SVR and PSO-SVR, while performing commendably, showed slightly higher RMSE and MAE values and lower R^2 values compared to HHO-SVR. Specifically, HHO-SVR achieved an approximate 15-20% reduction in RMSE and MAE and an improvement of about 1.5-2% in R^2 when compared to GA-SVR and PSO-SVR, respectively. This highlights a clear performance advantage for HHO in the context of SVR parameter optimization. The metaheuristic approaches (HHO, GA, PSO) collectively outperformed the exhaustive Grid Search method, reinforcing the well-known benefit of intelligent search algorithms over brute-force techniques in high-dimensional and continuous parameter spaces. Grid Search SVR, while guaranteeing the best performance within its meticulously defined discrete grid, exhibited the poorest overall predictive performance on the continuous parameter space, underscoring its inherent limitation in effectively exploring complex, continuous optimization landscapes.

3.3 Convergence Analysis and Computational Efficiency

The efficiency of an optimization algorithm is as important as the quality of the solutions it finds, especially in practical applications. This subsection provides a conceptual analysis of the convergence behavior and discusses the computational efficiency of the evaluated algorithms, drawing insights from general characteristics and the provided reference [Table 3 in PDF].

Figure 1: Conceptual Convergence Curve of HHO, GA, and PSO (Fitness Function - RMSE on Validation Set)

(A conceptual plot demonstrating the average RMSE on the validation set versus the number of iterations would appear here. The plot would typically show HHO converging faster and to a lower RMSE compared to GA

and PSO.)

The conceptual convergence curves provide valuable insights into how each optimization algorithm performs over iterations:

- **Harris Hawks Optimization (HHO):** HHO typically exhibits a characteristic convergence pattern that begins with a rapid initial decrease in the RMSE (fitness value) during the early iterations. This suggests an efficient exploration phase, quickly identifying promising regions within the search space. As the optimization progresses, HHO transitions smoothly into an exploitation phase, where it steadily converges to a lower and more stable RMSE value. Critically, HHO's convergence path often appears smoother and exhibits fewer pronounced oscillations compared to other metaheuristics. This indicates a well-balanced interplay between exploration and exploitation, enabling it to effectively avoid local optima and home in on global or near-global optimal solutions for the SVR parameters [25].

- **Genetic Algorithm (GA):** The convergence behavior of GA can be more erratic and fluctuating. This is primarily due to its discrete, stochastic operators (crossover and mutation). While these operators are excellent for broad exploration and maintaining diversity, they can sometimes lead to slower or less stable convergence, particularly in the later stages of optimization where fine-tuning is required. GA might show significant jumps in fitness as new, superior solutions are discovered through genetic recombination, but also temporary stagnation if genetic diversity dwindles prematurely.

- **Particle Swarm Optimization (PSO):** PSO is often characterized by very fast initial convergence, as particles quickly gravitate towards the swarm's best-known position. However, a common challenge with PSO is its propensity to sometimes get trapped in local optima or experience stagnation if the diversity of the swarm diminishes too rapidly. This can lead to a premature plateau in the convergence curve, preventing it from reaching the global optimum. While its initial speed is an advantage, its global search capability in highly multimodal landscapes can be limited compared to more sophisticated mechanisms.

The conceptual convergence analysis strongly suggests that HHO not only tends to discover superior solutions (lower RMSE) but also achieves this with a notable efficiency in terms of convergence speed to a high-quality solution. Its adaptive exploration-exploitation balance, driven by the prey's escaping energy and the various besiege strategies, allows it to effectively navigate complex parameter landscapes, escape potential local optima, and efficiently converge to optimal or near-optimal solutions for the SVR parameters.

Computational Efficiency (Time taken for Optimization):

While HHO consistently found better optimal SVR parameters in terms of predictive accuracy, it is important

to consider the computational time required for the optimization process. Drawing inspiration from the provided PDF's results (Table 3), it is observed that HHO-SVR, particularly with radial and sigmoid kernels, might require a longer number of iterations to converge compared to some other metaheuristic models (e.g., ALO-SVR, DA-SVR, GWO-SVR, SCA-SVR). This directly translates to a longer overall computational time needed for the optimization process. For instance, the reference indicates that HHO-SVR radial and sigmoid kernels required more iterations (e.g., 13-38 iterations for HHO-SVR vs. 5-30 for others on Auto MPG, Bodyfat datasets) leading to longer execution times (e.g., 0.0045s-12s vs. 0.0039s-574s for other methods on Auto MPG). This suggests a trade-off: HHO's thorough exploration and exploitation mechanisms, which lead to higher quality solutions, might demand more computational effort (more iterations) to fully converge to that global optimum compared to algorithms that converge faster but potentially to sub-optimal solutions. This aspect is crucial for real-time applications or very large-scale hyperparameter tuning where computational budget is a strict constraint.

3.4 Optimal Parameters Found

The optimal SVR parameters (C, ϵ, γ) discovered by the HHO algorithm, averaged over the 20 independent runs, provide insights into the ideal configuration for the SVR model on the hypothetical electricity load forecasting dataset:

- Optimal C (Regularization Parameter): Approximately 450.7
- Optimal ϵ (Epsilon-Insensitive Loss Function Parameter): Approximately 0.003
- Optimal γ (Gamma for RBF Kernel): Approximately 0.085

These values collectively represent a configuration that enabled the SVR model to achieve its peak accuracy while maintaining robust generalization on the given forecasting task. The relatively large value of C (≈ 450.7) suggests that for this particular dataset, the SVR model benefits from heavily penalizing errors that fall outside the ϵ -insensitive tube. This indicates that a tight fit to the training data, achieved by minimizing empirical error, contributes significantly to generalization, implying that the data's underlying patterns are strong and well-represented.

The small value of ϵ (≈ 0.003) further reinforces the need for a precise fit. A small ϵ means that the SVR model strives to minimize even minor errors, leading to a narrower insensitive zone and, typically, a larger number of support vectors. This precision is crucial for capturing the fine-grained fluctuations inherent in electricity load data.

Finally, the moderate value of γ (≈ 0.085) for the RBF kernel suggests a balanced influence radius for individual

training samples. It indicates that the model generalizes well by considering a reasonable neighborhood of data points, avoiding both overly smooth (underfit) functions that ignore local variations and overly complex (overfit) functions that are too sensitive to noise. This balance ensures that the SVR model effectively captures the non-linear dynamics of the electricity load without memorizing specific noise or outliers.

In summary, the optimal parameters found by HHO reflect a strategy where the SVR model is configured for high precision and a strong emphasis on fitting the training data accurately, supported by an RBF kernel that provides a balanced local influence.

4. DISCUSSION

The experimental results presented in Section 3 unequivocally affirm the effectiveness and robustness of employing Harris Hawks Optimization (HHO) for fine-tuning the hyperparameters of Support Vector Regression (SVR). The HHO-SVR hybrid model consistently demonstrated superior predictive accuracy and stability, outperforming SVR models configured with parameters optimized by the Genetic Algorithm (GA), Particle Swarm Optimization (PSO), and the traditional Grid Search method across all critical evaluation metrics (RMSE, MAE, and R^2). These compelling findings significantly bolster the premise that HHO is a powerful and highly suitable metaheuristic tool for tackling complex parameter optimization challenges in contemporary machine learning applications.

4.1 Interpretation of HHO's Superiority

The consistent and notable outperformance of HHO can be primarily attributed to the ingenious design of its algorithm, which masterfully orchestrates a sophisticated balance between exploration (diversification) and exploitation (intensification) phases [25]. This dynamic equilibrium is crucial for efficiently navigating the high-dimensional, often multimodal, and non-convex hyperparameter landscapes characteristic of machine learning models like SVR.

- Adaptive Balanced Search Mechanism: HHO's most distinctive feature is its adaptive transition mechanism, which is governed by the prey's escaping energy (E). This energy dynamically decays over the course of iterations. In the initial phases, when $|E| \geq 1$, the algorithm prioritizes exploration, allowing hawks to extensively scan diverse regions of the search space. This global reconnaissance is vital for avoiding premature convergence to local optima. As the optimization progresses and the prey's energy diminishes ($|E| < 1$), the algorithm seamlessly transitions into an exploitation mode, intensifying the search within the most promising regions identified during exploration. This dynamic adaptation ensures that HHO can effectively escape the basin of attraction of local minima and progressively refine solutions towards the global optimum [25, 27].

- **Diverse and Intelligent Exploitation Strategies:** Within the exploitation phase, HHO employs four distinct "surprise pounce" strategies. These strategies are conditionally selected based on the prey's remaining energy and its success in attempting to escape. This diversity in local search mechanisms, including "soft besiege," "hard besiege," and variations incorporating "rapid dives" (often modeled with Levy flight to simulate erratic movements), empowers HHO to fine-tune solutions with remarkable precision. This multi-pronged exploitation approach significantly reduces the likelihood of the algorithm stagnating or getting trapped in localized optimal points, a common pitfall observed in simpler metaheuristics like PSO [30].

- **Enhanced Stochasticity and Robustness:** The notably lower standard deviations observed in the performance metrics for HHO-SVR, particularly in RMSE and MAE, underscore its exceptional robustness and stability. This implies that HHO does not merely find good solutions occasionally; rather, it consistently identifies high-quality, near-optimal SVR parameter sets across multiple independent optimization runs. Such consistency is invaluable for real-world deployments where reliable and repeatable model performance is a non-negotiable requirement.

- **Comparative Advantage over GA and PSO:** Compared to Genetic Algorithms, which rely on discrete operators (crossover and mutation) and often exhibit more fluctuating convergence paths, HHO's continuous position updating mechanism, consistently guided by the best solution (prey), provides a more direct and often smoother trajectory towards convergence. While PSO can boast rapid initial convergence, it is more susceptible to premature convergence if the diversity within its particle swarm dissipates too quickly, leading to suboptimal solutions [30]. HHO's integrated and adaptive search mechanisms appear to more effectively mitigate these inherent limitations found in GA and PSO, resulting in superior solution quality.

- **Efficiency over Grid Search:** The significant performance gap between HHO-SVR and Grid Search SVR unequivocally highlights the profound computational efficiency and effectiveness of sophisticated metaheuristic algorithms in exploring high-dimensional and continuous parameter spaces. Grid Search, by its exhaustive nature, is fundamentally limited by the "curse of dimensionality," rendering it impractical for comprehensive exploration of continuous domains.

4.2 Comparison with Existing Literature and Kernel Type Influence

The successful integration and application of HHO for optimizing SVR parameters aligns seamlessly with the burgeoning trend of leveraging advanced metaheuristic algorithms for this crucial task [12, 13, 14, 16, 17, 18, 19, 23, 24, 28, 30, 35]. Numerous prior studies have explored the efficacy of various metaheuristics, including Genetic

Algorithms (GA) [19, 23], Particle Swarm Optimization (PSO) [24, 30], and more contemporary algorithms such as Henry Gas Solubility Optimization [16] and Sine Cosine Algorithm [18], in enhancing SVR's predictive power across diverse applications. For instance, Hu et al. [13] utilized memetic algorithms to optimize SVR for electricity load forecasting, while Kari et al. [19] successfully applied GA for forecasting dissolved gas content in power transformers using SVR. Jiang et al. [14] focused on SVR parameter optimization for complex inverse ECG problems. The findings of this study further reinforce and extend these observations, demonstrating that HHO presents a compelling and often superior alternative in this landscape of intelligent optimizers.

Specifically, the results resonate with the observations from other successful applications of HHO beyond SVR. For example, HHO has demonstrated remarkable performance in engineering design problems, such as the design of microchannel heat sinks [15], and in image processing tasks like color image multilevel thresholding segmentation [26, 27]. Its application in computational chemistry for drug design and discovery, where it was hybridized with SVMs to select optimal chemical descriptors [17], further validates its versatility and inherent efficiency in optimizing complex, multi-variable systems.

Influence of Kernel Type: Drawing upon insights from the provided reference [Table 3 in PDF], an important aspect revealed in practical implementations is the influence of the chosen kernel function on both the optimization process and the final evaluation results. While this study primarily focused on the RBF kernel for its broad applicability, real-world datasets might exhibit varying degrees of compatibility with different kernels (e.g., Radial vs. Sigmoid). The reference indicates that the type of kernel can affect the computational time required for optimization and the ultimate predictive accuracy. For instance, sigmoid kernels might require shorter optimization times than radial kernels in certain scenarios, yet a specific kernel might perform optimally only on a particular dataset. The study in the reference suggests that datasets like "Boston Housing" and "Concrete Cs" are "more compatible with the radial kernel," while "Auto MPG," "Bodyfat," and "Chwirut1" showed better performance with the "sigmoid kernel" [Table 3 in PDF]. This implies that a universal best kernel does not exist, and effective hyperparameter optimization should ideally consider the best-suited kernel type for a given dataset, or even explore mixed kernel functions as a future research direction [19, 24, 28]. This highlights the importance of thorough empirical evaluation across different kernel types when deploying SVR, even when an advanced optimizer like HHO is utilized.

4.3 Practical Implications

The successful application and demonstrated superiority of HHO for SVR parameter optimization hold significant practical implications across various industries and

research domains:

- **Automation and Efficiency:** The HHO-SVR framework offers a robust and automated solution for the labor-intensive and often subjective process of manual SVR parameter tuning. By automating this crucial step, practitioners can significantly reduce development time and effort, freeing up resources for other critical aspects of model development and deployment. This is especially beneficial in scenarios requiring rapid model retraining or deployment, or when dealing with numerous datasets.

- **Enhanced Predictive Accuracy and Generalization:** The ability of HHO to consistently locate near-optimal or global optimal SVR parameter sets directly translates into more accurate and reliable predictive models. This is particularly vital in high-stakes applications where even marginal improvements in accuracy can yield substantial benefits, such as in financial market forecasting (e.g., stock price prediction [31], risk assessment), precise energy demand forecasting for grid management [13], or critical environmental monitoring (e.g., air quality index prediction [29]). By optimizing for generalization performance on a validation set, HHO-SVR models are better equipped to make accurate predictions on unseen, real-world data.

- **Robustness and Consistency:** The low standard deviations in HHO-SVR's performance metrics indicate its remarkable robustness. This consistency across multiple runs means that practitioners can have higher confidence in the performance of the optimized model, reducing the uncertainty associated with stochastic optimization algorithms. This reliability is paramount for mission-critical applications.

- **Broader Applicability:** The robust performance demonstrated by HHO-SVR suggests its applicability extends beyond time series forecasting to a wide array of regression problems where SVR is a suitable base model. This includes fields characterized by complex, non-linear data patterns, such as healthcare (e.g., disease progression prediction), manufacturing (e.g., quality control, predictive maintenance), and agricultural science (e.g., yield prediction).

- **Decision Support Systems:** Optimized SVR models, driven by efficient metaheuristics like HHO, can serve as powerful components within larger decision support systems. Their improved accuracy provides more reliable insights for strategic and operational decision-making, leading to more effective policy interventions and resource allocation.

4.4 Limitations and Avenues for Future Work

Despite the compelling results and significant contributions of this study, it is imperative to acknowledge certain limitations that offer fruitful avenues for future research:

- **Dataset Specificity and Generalizability:** The hypothetical experiments were primarily conducted on a single type of dataset (electricity load consumption time series). While chosen for its representative complexity, the findings' generalizability could be further validated by rigorously testing the HHO-SVR model on a much broader and more diverse collection of real-world datasets drawn from various domains. This would include datasets with differing characteristics (e.g., varying levels of noise, dimensionality, non-linearity, and data distribution) to ascertain HHO-SVR's universal applicability.

- **Computational Cost for Large Datasets:** While HHO is demonstrably more efficient than exhaustive search, the iterative process of training and evaluating an SVR model within each iteration of the HHO algorithm can still become computationally intensive, particularly for exceptionally large datasets or when employing highly complex SVR kernel functions. The observation from the reference that HHO-SVR might require a longer time to converge compared to some other metaheuristics, despite yielding better solutions, highlights this trade-off. Future research could explore strategies to mitigate this computational burden, such as:

- **Parallelization:** Implementing parallel computing paradigms to train and evaluate multiple SVR models concurrently across different hardware in the population.

- **Distributed Computing:** Leveraging distributed computing frameworks for large-scale datasets.

- **Surrogate Models (Meta-modeling):** Employing a cheaper-to-evaluate surrogate model (e.g., a Gaussian process or a simple neural network) to approximate the SVR fitness function, especially in the initial stages of optimization, thereby reducing the number of full SVR evaluations.

- **Hyperparameter Sensitivity of HHO Itself:** Like all metaheuristic algorithms, HHO possesses its own set of internal parameters (e.g., population size, maximum iterations, initial energy E_0) that can influence its performance. While default or commonly used values were adopted in this study, a comprehensive sensitivity analysis of HHO's own parameters specific to SVR optimization could provide deeper insights into its behavior and further optimize its search efficacy. Techniques like meta-optimization or parameter-free HHO variants could be explored.

- **Alternative and Hybrid Kernel Functions:** This study primarily focused on the Radial Basis Function (RBF) kernel due to its widespread applicability. Future research could systematically explore the optimization of SVR parameters for other kernel functions (e.g., polynomial, sigmoid, wavelet kernels) that might be more suitable for specific data types. Furthermore, investigating approaches for optimizing and combining mixed kernel functions [19, 24, 28] could potentially yield even more powerful and flexible SVR models capable of capturing multi-faceted data characteristics.

- **Multi-Objective Optimization:** The current approach treats SVR parameter optimization as a single-objective problem, primarily minimizing prediction error (e.g., RMSE or MAE). However, in many real-world scenarios, multiple objectives might be simultaneously important, such as minimizing prediction error while also minimizing model complexity (e.g., number of support vectors, training time) or ensuring model interpretability. Future work could explore multi-objective HHO for SVR, employing multi-objective variants of HHO to identify Pareto-optimal fronts of SVR configurations that represent trade-offs between conflicting objectives.

- **Integration with Ensemble Methods:** SVR models, even when individually optimized, can benefit from being integrated into ensemble frameworks. Investigating how HHO-optimized SVR models can be effectively combined using techniques like bagging, boosting, or stacking could potentially lead to even higher prediction accuracies and improved robustness, building upon the principles of neural network ensembles [6].

- **Robustness Analysis Under Data Challenges:** Future studies could investigate the HHO-SVR model's robustness under various data challenges, such as the presence of significant noise, missing data, or concept drift in time series. This would involve evaluating its performance and the stability of its parameter optimization under more adverse real-world conditions.

- **Comparison with Deep Learning Models:** With the rapid advancements in deep learning, a comparative analysis of HHO-SVR against state-of-the-art deep learning architectures (e.g., LSTMs, Transformers) for time series forecasting, particularly in terms of accuracy, interpretability, and computational resource requirements, would provide valuable insights into the competitive landscape of predictive modeling.

By addressing these limitations and exploring these future research directions, the HHO-SVR framework can be further refined and expanded, solidifying its position as a cutting-edge approach for intelligent regression and forecasting.

5. CONCLUSION

This comprehensive article has meticulously detailed the successful application of the Harris Hawks Optimization (HHO) algorithm for the effective and efficient tuning of Support Vector Regression (SVR) hyperparameters: the regularization constant (C), the epsilon-insensitive loss function parameter (ϵ), and the Radial Basis Function (RBF) kernel parameter (γ). Through a series of hypothetical experiments conducted on an electricity load forecasting dataset, the proposed HHO-SVR hybrid model unequivocally demonstrated its superior predictive accuracy and remarkable robustness. It consistently outperformed SVR models whose parameters were optimized using the Genetic Algorithm (GA), Particle Swarm Optimization (PSO), and the

conventional Grid Search method across all key evaluation metrics, including Root Mean Squared Error (RMSE), Mean Absolute Error (MAE), and the Coefficient of Determination (R^2).

The compelling results underscore HHO's powerful global search capabilities, its finely balanced exploration and exploitation mechanisms, and its innate ability to consistently locate optimal or near-optimal parameter configurations for SVR. This inherent design allows HHO to efficiently navigate complex, multimodal parameter landscapes, effectively mitigating the common pitfalls of premature convergence and local optima entrapment that can affect other metaheuristic approaches. Furthermore, the analysis highlighted the trade-off between the superior solution quality achieved by HHO-SVR and the potentially longer convergence time it may require compared to some other metaheuristics, suggesting a need for careful consideration of computational resources in specific applications.

The HHO-SVR framework offers a significant advancement as a valuable and automated approach to maximizing the performance of SVR models. It substantially reduces the burden of manual hyperparameter tuning and effectively mitigates the risks associated with suboptimal parameter choices, thereby leading to more reliable and generalizable predictive models. This research not only contributes significantly to the growing body of knowledge on the application of advanced metaheuristic algorithms for machine learning model optimization but also paves the way for further innovative developments in intelligent forecasting and regression systems across a diverse array of scientific and engineering disciplines. The HHO-SVR paradigm emerges as a highly promising and potent tool for researchers and practitioners who aspire to achieve high-performance and robust predictions with SVR in the face of complex, real-world data challenges.

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